



# RADIO INTERFEROMETRIC IMAGING

The fun of Fourier Transforms...

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Talk credits: J. Radcliffe, based on A. Offringa's & N. Jackson's 2015 ERIS talks and T. Muxlow's 2013 ERIS talk

Hi, Dr. Elizabeth?  
Yeah, uh... I accidentally took  
the Fourier transform of my cat...





# OUTLINE

1. Deconvolution
  - CLEAN
  - Windowing
  - CASA clean/tclean
2. Data gridding & weighting
  - uv weighting
  - Telescope weighting
3. Wide-field imaging limits
  - Smearing
  - Non-coplanar baselines
  - Primary beam
4. Signal to noise & dynamic range

# 1. DECONVOLUTION

The basic operation of an (ideal) interferometer baseline measures (small sky approximation,  $w \rightarrow 0$ ):

$$V(u, v) \approx \iint I(l, m) e^{-2\pi i(ul + vm)} dl dm$$

We can, in principle, measure  $I(l, m)$  for all  $u, v$ . We can then use a Fourier transform to recover the sky brightness distribution:

$$I(l, m) \approx \iint V(u, v) e^{2\pi i(ul + vm)} du dv$$

However  $V(u, v)$  is not known everywhere but is sampled at particular places on the  $u$ - $v$  plane

Nb:  $(l, m, n)$  notation is essentially the same as  $(x, y, z)$  coordinates used in the prev. talks

# DECONVOLUTION

This sampling function can be described by  $S(u,v)$  and is equal to 1 when the  $uv$  plane is sampled and zero otherwise:

$$I^D(l, m) = \iint V(u, v) S(u, v) e^{2\pi i(ul+vm)} du dv$$

$I^D(l,m)$  is known as the **'dirty image'** and is related to the real sky brightness distribution by (using convolution theorem of FT):

$$I^D(l, m) = I(l, m) * B$$

Where  $B$  is known as the **'dirty beam'** or the **'point spread function'** and is the FT of the sampling function.

$$B(l, m) = \iint S(u, v) e^{2\pi i(ul+vm)} du dv$$

# CASA IMAGE CONSTRUCTION

```
# tclean :: Radio Interferometric Image Reconstruction
vis = '' # Name of input visibility file(s)
selectdata = True # Enable data selection parameters
  field = '' # field(s) to select
  spw = '' # spw(s)/channels to select
  timerange = '' # Range of time to select from data
  uvrange = '' # Select data within uvrange
  antenna = '' # Select data based on antenna/baseline
  scan = '' # Scan number range
  observation = '' # Observation ID range
  intent = '' # Scan Intent(s)

datacolumn = 'corrected' # Data column to image(data,corrected)
imagename = '' # Pre-name of output images
imsize = [256, 256] # Number of pixels
cell = ['1.0arcsec'] # Cell size
phasecenter = '' # Phase center of the image
stokes = 'I' # Stokes Planes to make
projection = 'SIN' # Coordinate projection (SIN, HPX)
startmodel = '' # Name of starting model image
specmode = 'mfs' # Spectral definition mode (mfs,cube,cubedata)
  reffreq = '' # Reference frequency

gridded = 'standard' # Gridding options (standard, wproject, widefield,
  mosaic, aproject)
  vptable = '' # Name of Voltage Pattern table
  pblimit = 0.2 # >PB gain level at which to cut off normalizations

deconvolver = 'hogbom' # Minor cycle algorithm
  (hogbom,clark,multiscale,mtmfs,mem,clarkstokes)
restoration = True # Do restoration steps (or not)
  restoringbeam = [''] # Restoring beam shape to use. Default is the PSF main
  lobe
  pbcor = False # Apply PB correction on the output restored image

outlierfile = '' # Name of outlier-field image definitions
weighting = 'natural' # Weighting scheme (natural,uniform,briggs)
  uv taper = False # uv-taper on outer baselines in uv-plane

niter = 500 # Maximum number of iterations
  gain = 0.1 # Loop gain
  threshold = '0.0mJy' # Stopping threshold
  nsigma = 0.0 # Multiplicative factor for rms-based threshold
  stopping
  cycleniter = -1 # Maximum number of minor-cycle iterations
  cyclefactor = 1.5 # Scaling on PSF sidelobe level to compute the minor-
  cycle stopping threshold.
  minpsffraction = 0.05 # PSF fraction that marks the max depth of cleaning in
  the minor cycle
  maxpsffraction = 0.8 # PSF fraction that marks the minimum depth of
  cleaning in the minor cycle
  interactive = False # Modify masks and parameters at runtime

usemask = 'user' # Type of mask(s) for deconvolution: user, pb, or
  auto-multithresh
  mask = [] # Mask (a list of image name(s) or region file(s) or
  region string(s) )
  pbmask = 0.0 # primary beam mask

restart = True # True : Re-use existing images. False : Increment
  imagename
savemodel = 'none' # Options to save model visibilities (none, virtual,
  modelcolumn)
calcrs = True # Calculate initial residual image
calcpfsf = True # Calculate PSF
parallel = False # Run major cycles in parallel
```

- tclean is the CASA imaging routine (this replaced clean in CASA v4.6 and earlier)
- To achieve a basic image, need to set:
  - vis - your data (measurement set)
  - imagename (output image)
  - niter - no. of CLEAN iterations (next slide)
  - imsize - size of the image in pixels (needs to be as small as possible to decrease computation time)
  - cell - angular extent of each pixel (need to adequately sample the psf)

Rule of thumb:

$$\text{cell} \sim \lambda_f / 3B$$

$\lambda_f$  - wavelength of highest frequency channel  
 $B$  - longest baseline length

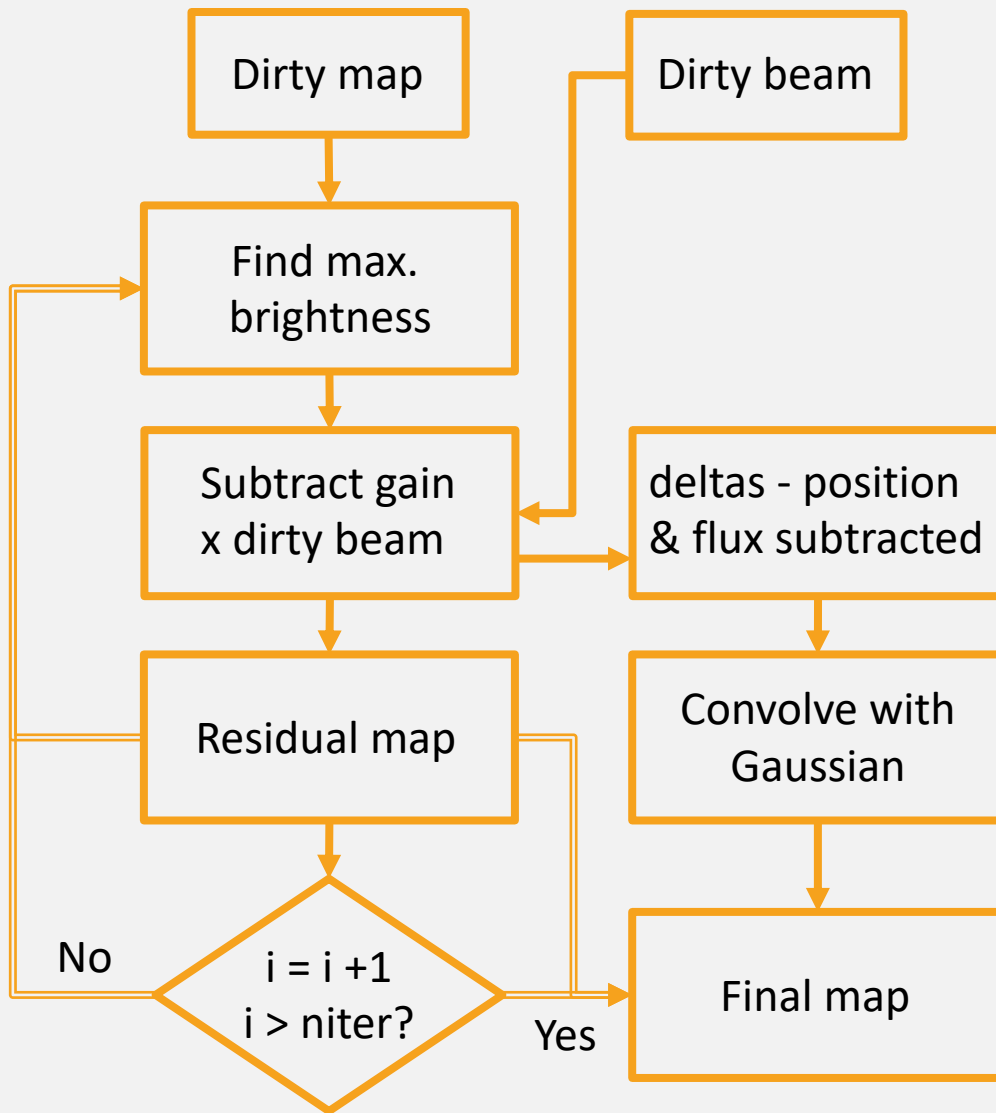
# DECONVOLUTION

To recover the real brightness distribution we just need to deconvolve...  
easier said than done:

- A vast number of images are consistent with the data inc. the dirty beam.
- We need to take a Bayesian approach - supply priors (i.e. extra information/ assumptions) so we can find the most probable brightness distribution.
- Simplest scheme (but not only): Sky is mostly **empty** and consists of a **finite number of unresolved point sources**.

→ The basis of the Hogbom CLEAN algorithm (1974)

# HOGBOM CLEAN & VARIANTS

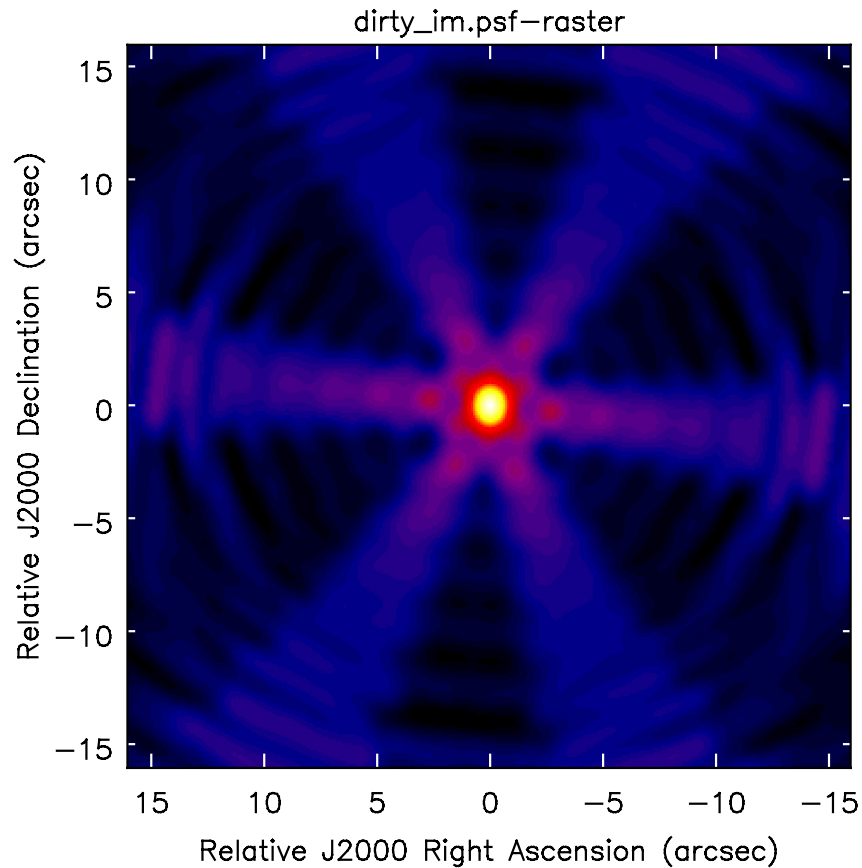


- A brute force deconvolution algorithm using the dirty beam
- Uses prior that the sky consists of unresolved point sources modelled by Dirac delta functions
- Other versions such as Clark, multiscale are variants of this algorithm

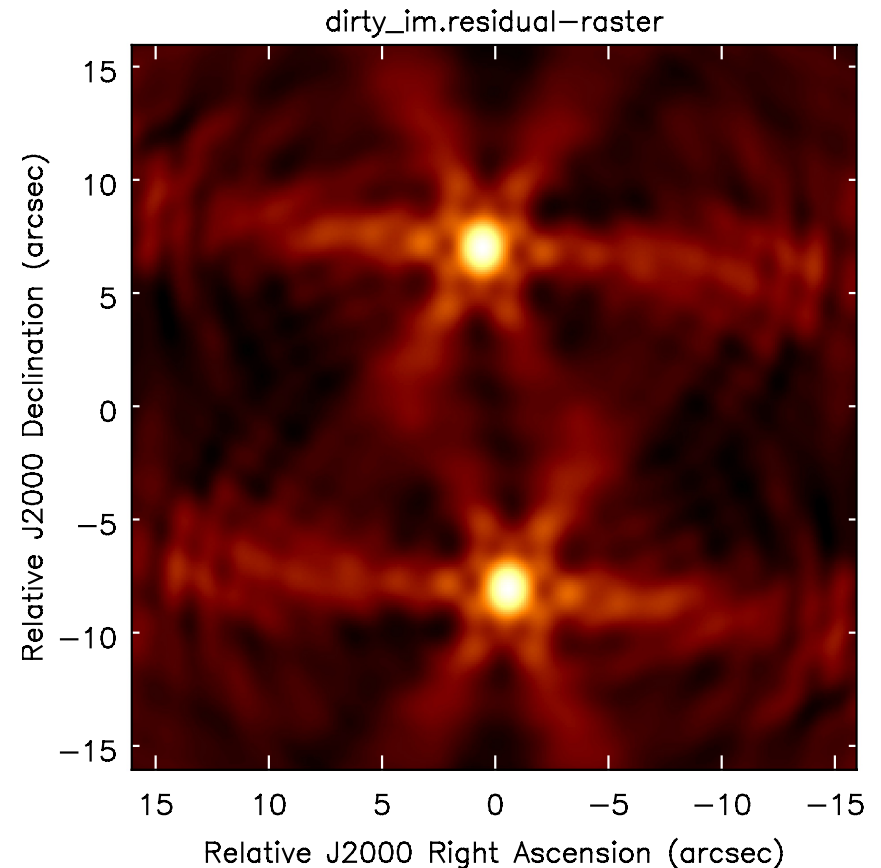
# CLEAN DECONVOLUTION

JVLA simulation, 2hr observation targeting two 0.1 Jy point sources + some phase corruption included

Dirty beam



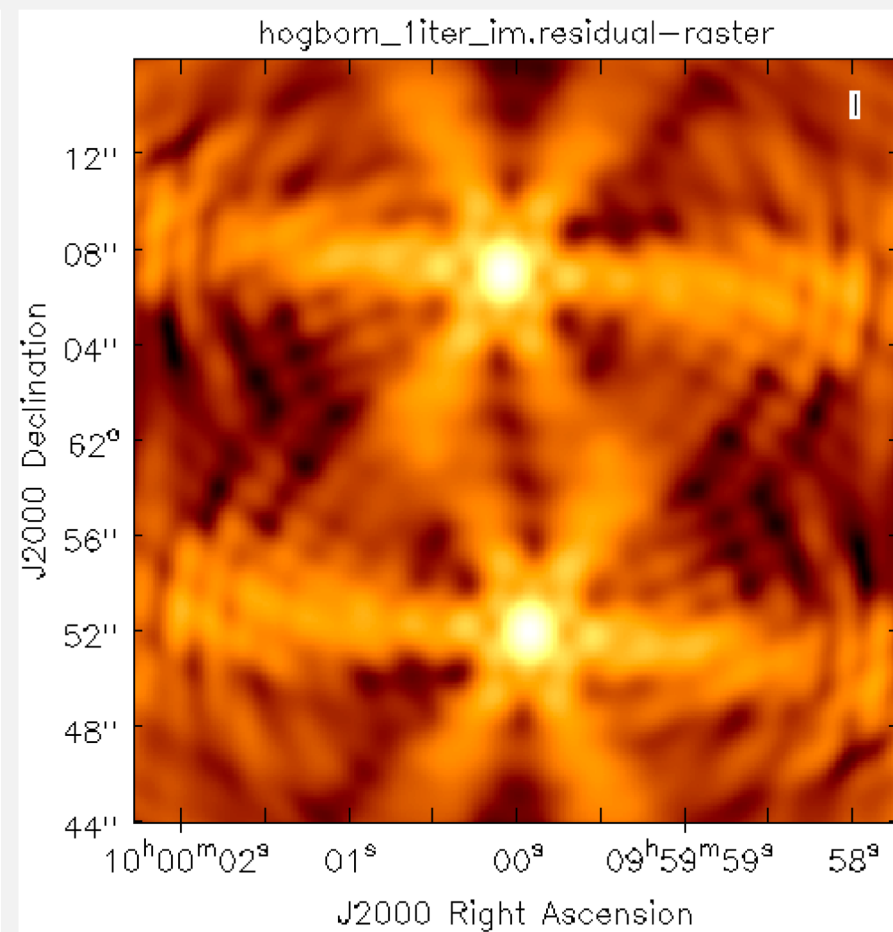
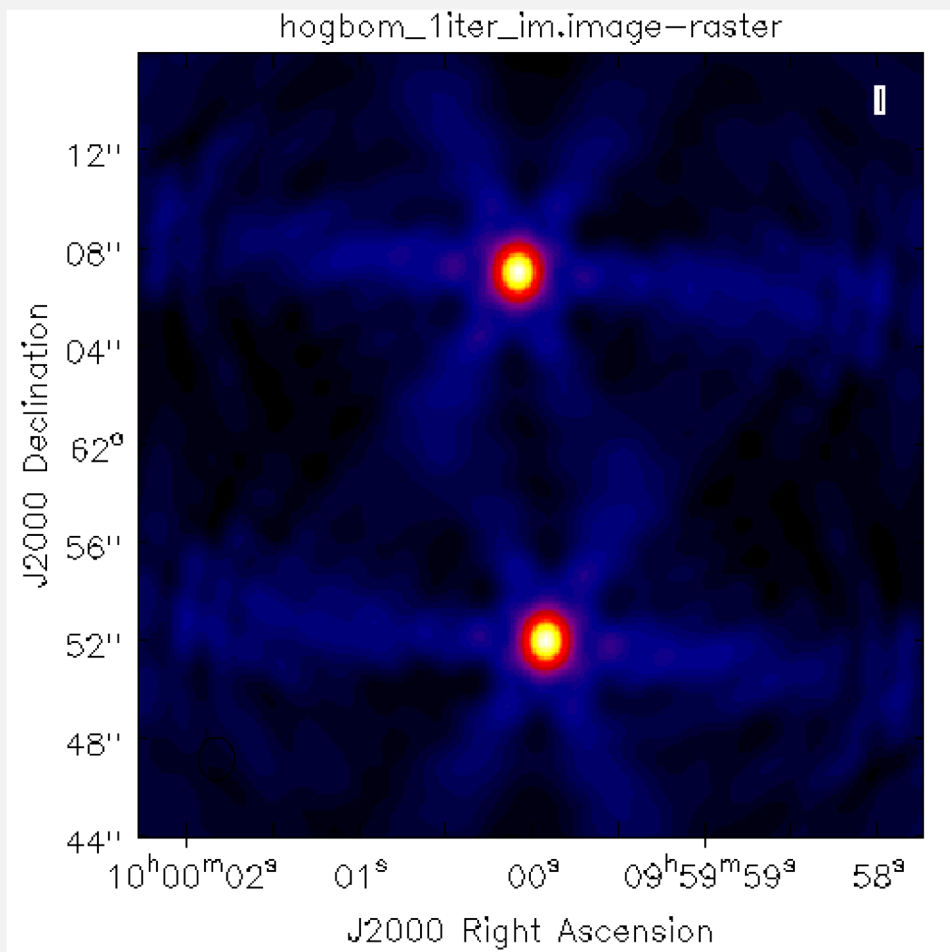
Dirty image



# CLEAN DECONVOLUTION

## Hogbom CLEAN

Image & residual after 1 iteration with 0.5 gain

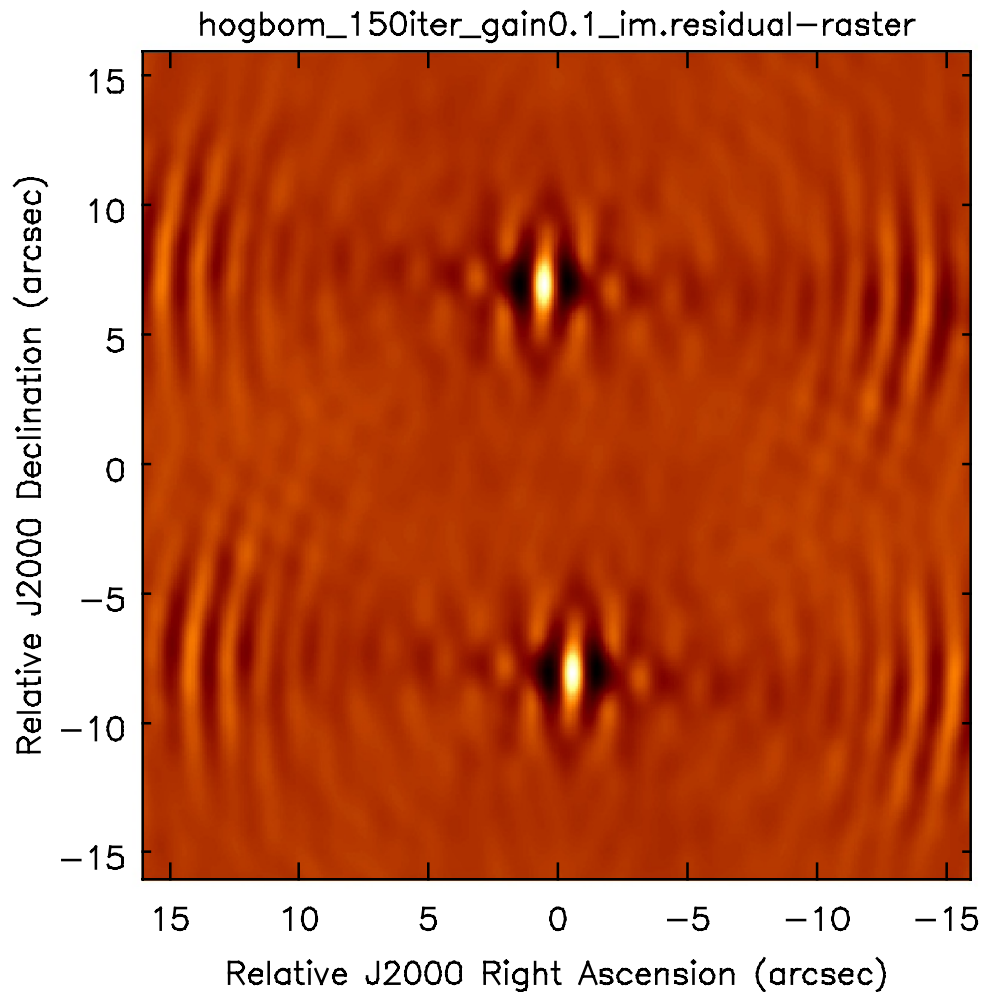




# CLEAN DECONVOLUTION

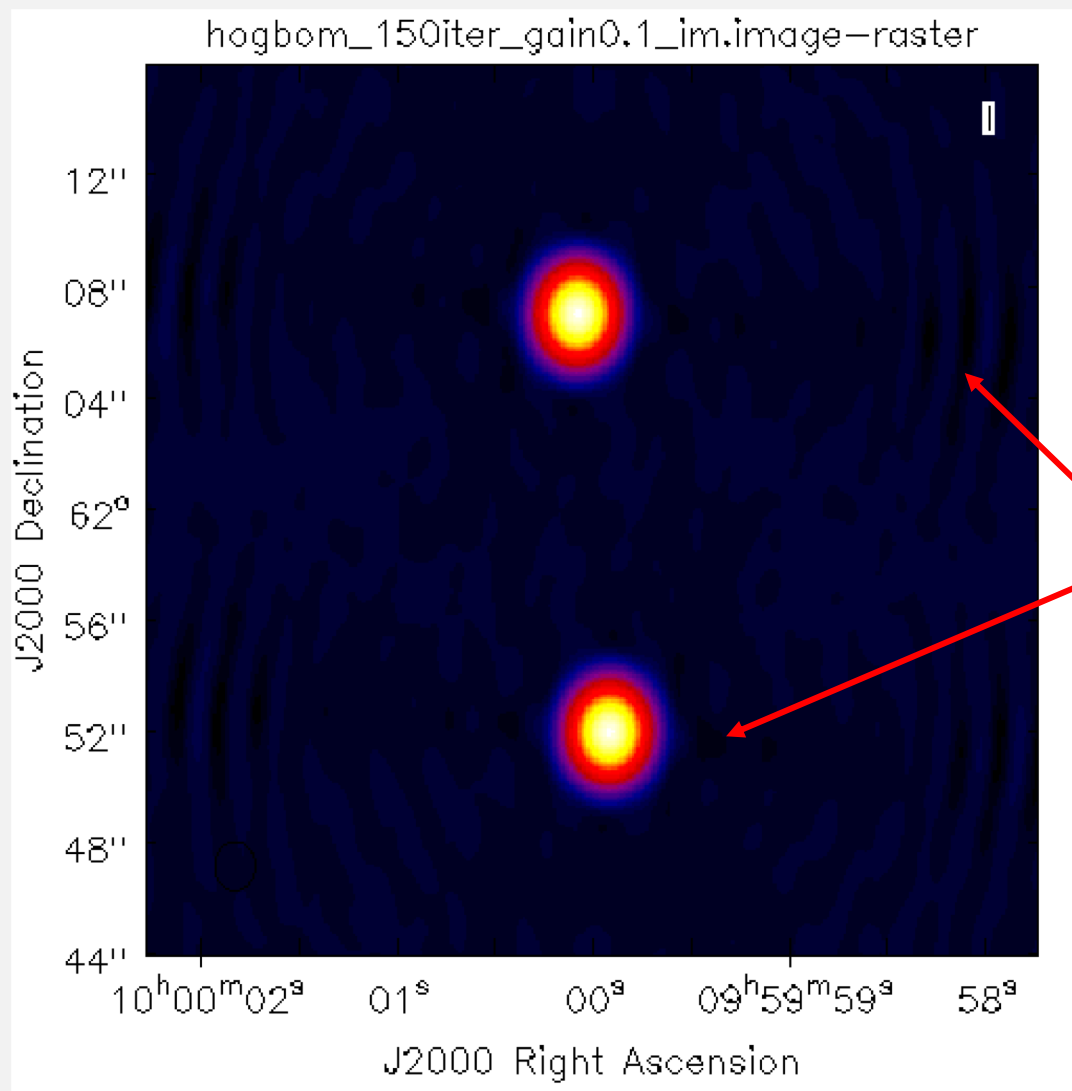
Hogbom CLEAN

Residual after 150 iterations with 0.1 gain



# CLEAN DECONVOLUTION

CLEAN map (residual+CLEAN components) after 150 iterations



Some  
artefacts left  
from  
deconvolution

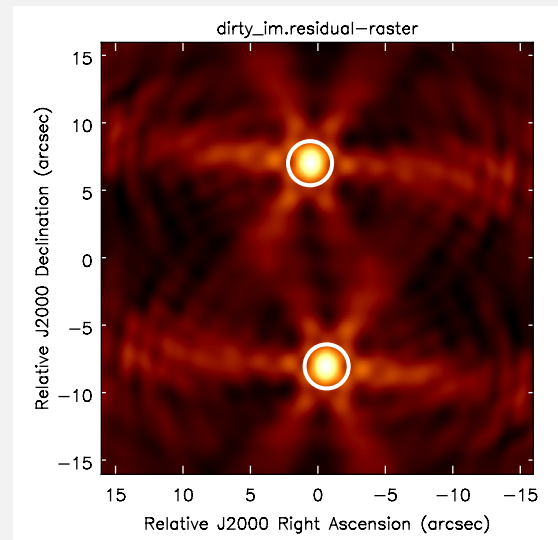
# CLEAN DECONVOLUTION

CLEAN is far from perfect, but we can lend it a hand:

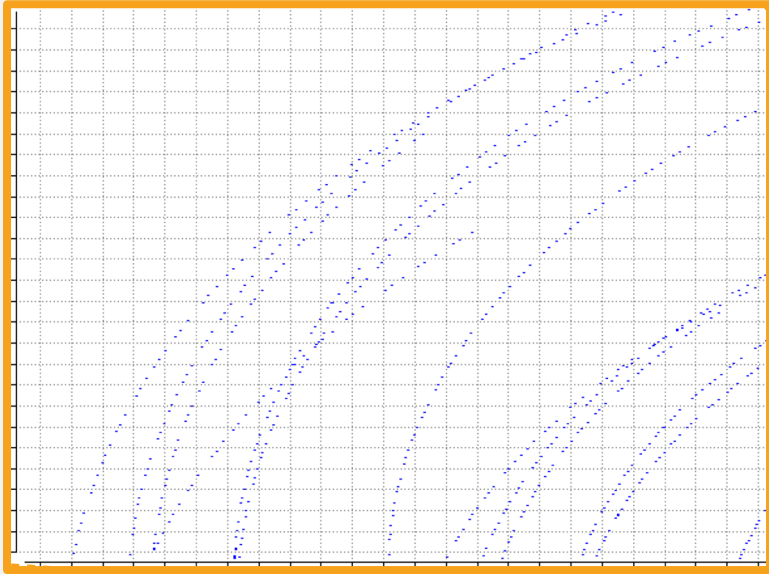
CLEAN consists of two 'cycles':

- I. Minor cycles - subtract subimages of the dirty beam
- II. Major cycles - Fourier Transform residual map and subtract

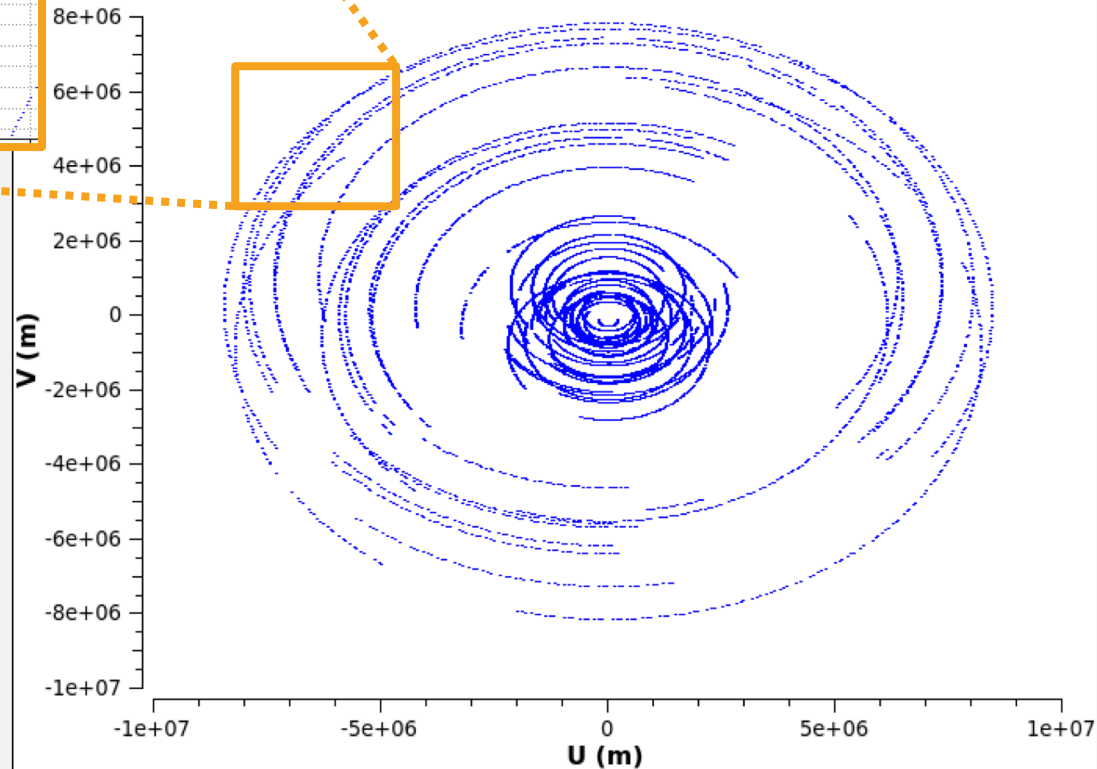
We can use windowing to tell the algorithm where the flux lies.  
This should be used when you **know** the flux you see is real!



## 2. WEIGHTING

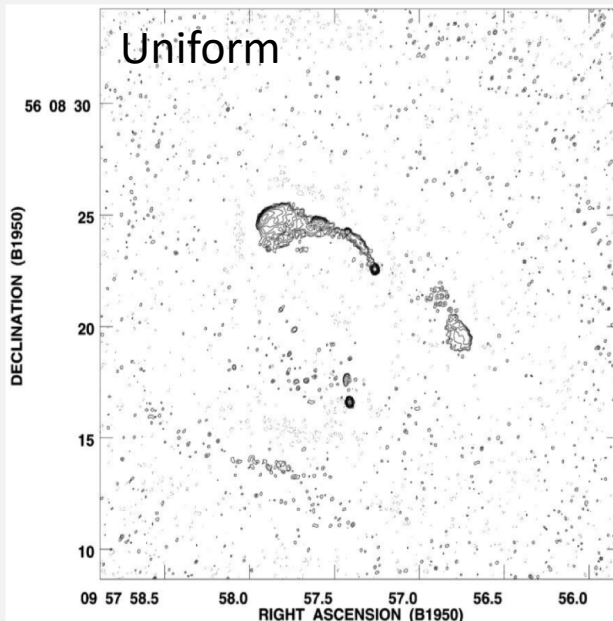
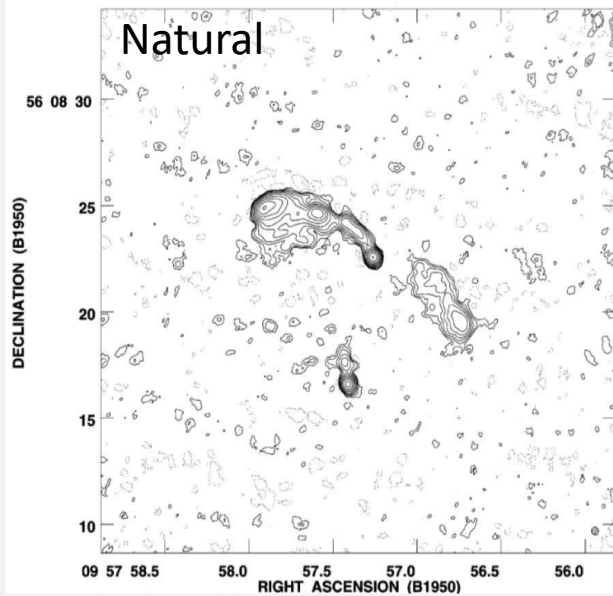


Integrations are distributed over a greater number of sampled grid points in the outer  $uv$  plane than the inner regions



- Data interpolated on  $2^n$  grid
- Weights unmodified by local density - 'Natural'
- Weights divided by local density of points - 'Uniform'

# UV WEIGHTING



Natural weighted images have low spatial frequencies are weighted up (due to gridding) and gives:

- Best S/N
- Worse resolution

Uniform weighted images low have spatial frequencies weighted down and the data are not utilised optimally (may be subject to a deconvolution striping instability) resulting in:

- Worse S/N
- Best resolution

Compromises exist:

- Briggs (robust) weighting parameter -5 to +5. (next slide)

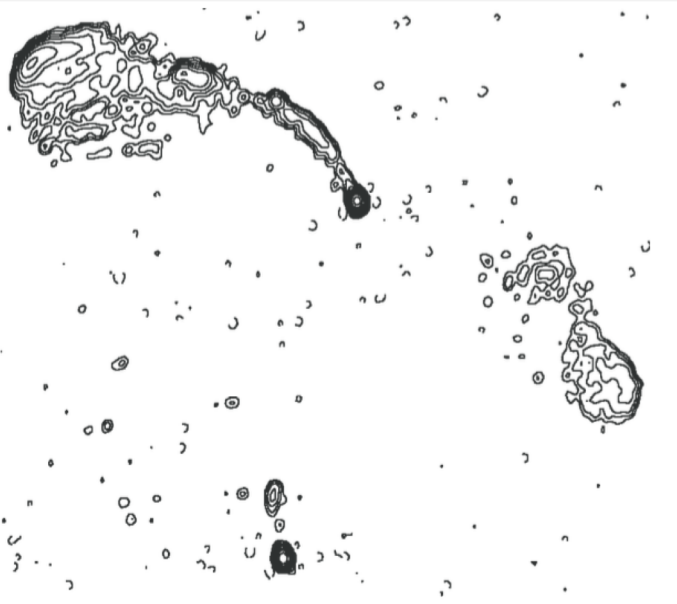
Implementation in CASA tclean/clean

```
weighting = 'natural' # Weighting of uv (natural, uniform,  
# briggs, ...)
```

## UV WEIGHTING: 'BRIGGS WEIGHTING'

- Originally derived as a cure for striping – Natural weighting is immune and therefore most 'robust'

Robust 0 image

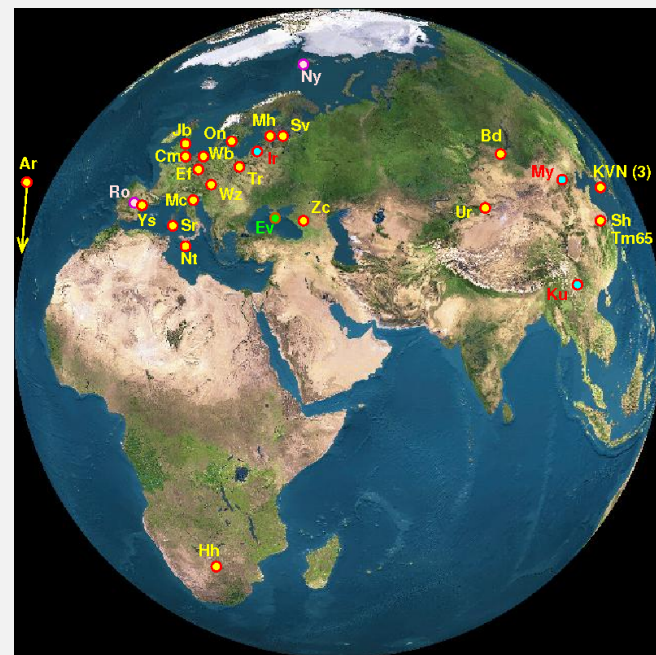


- Varies effective weighting as a function of local u-v weight density
  - Where weight density is low – effective weighting is natural
  - Where weight density is high – effective weighting is uniform
- Modifies the variations in effective weight found in uniform weighting → more efficient use of data & lower thermal noise
- ROBUST = - 5 is nearly pure uniform ROBUST = + 5 is nearly pure natural  
ROBUST = 0 is a good compromise (Contoured)
- Can produce images close to uniform weighting resolution with noise levels close to natural weighting. See CASA [webpage](#) for other weighting schemes!



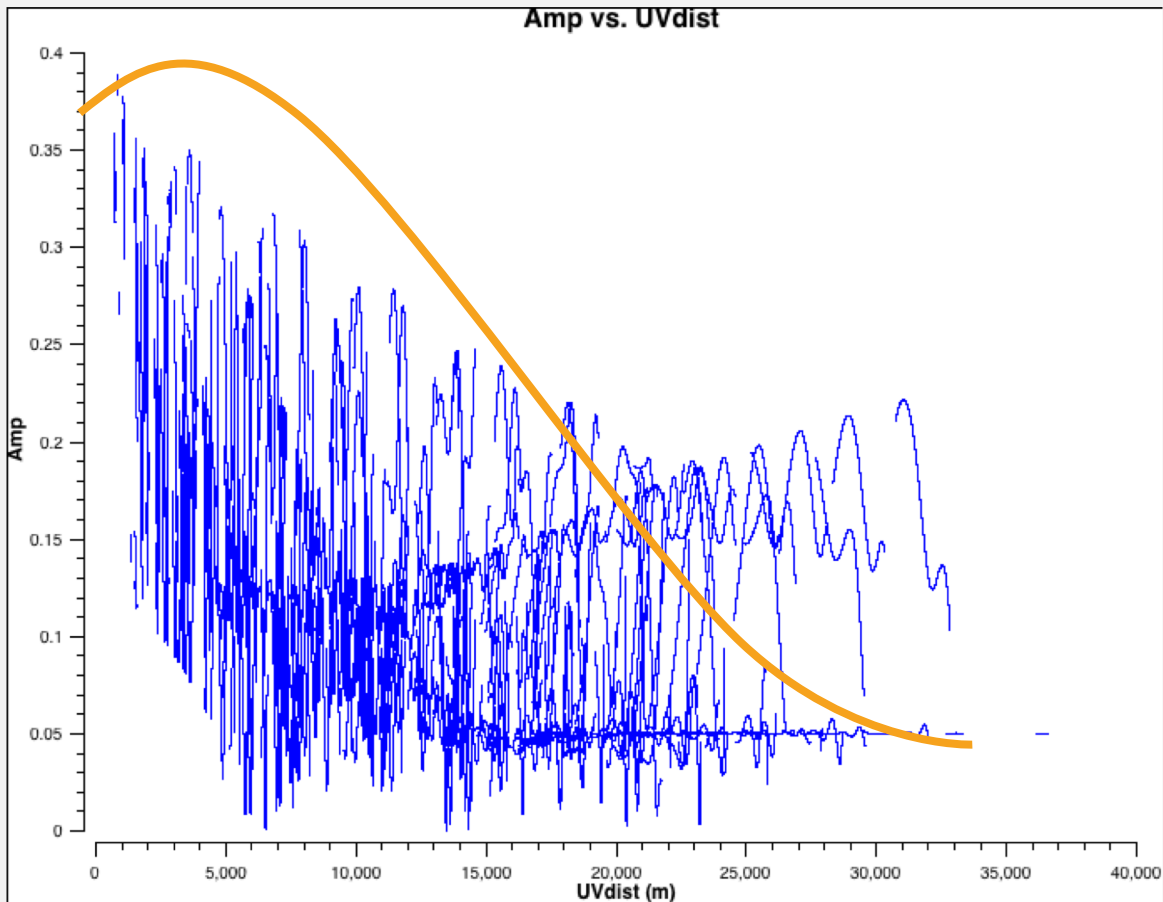
## WEIGHTING BY TELESCOPE

- Many arrays are heterogeneous e.g. e-MERLIN, EVN & AVN (when built)
- To get the best S/N need to increase weighting on larger telescopes so they contribute more.
- Nb. this can change the resolution depending on the baseline distribution.



# UV TAPERING

Gaussian  $u$ - $v$  taper or  $u$ - $v$  range can smooth the image but at the expense of sensitivity since data are excluded or data usage is non-optimal



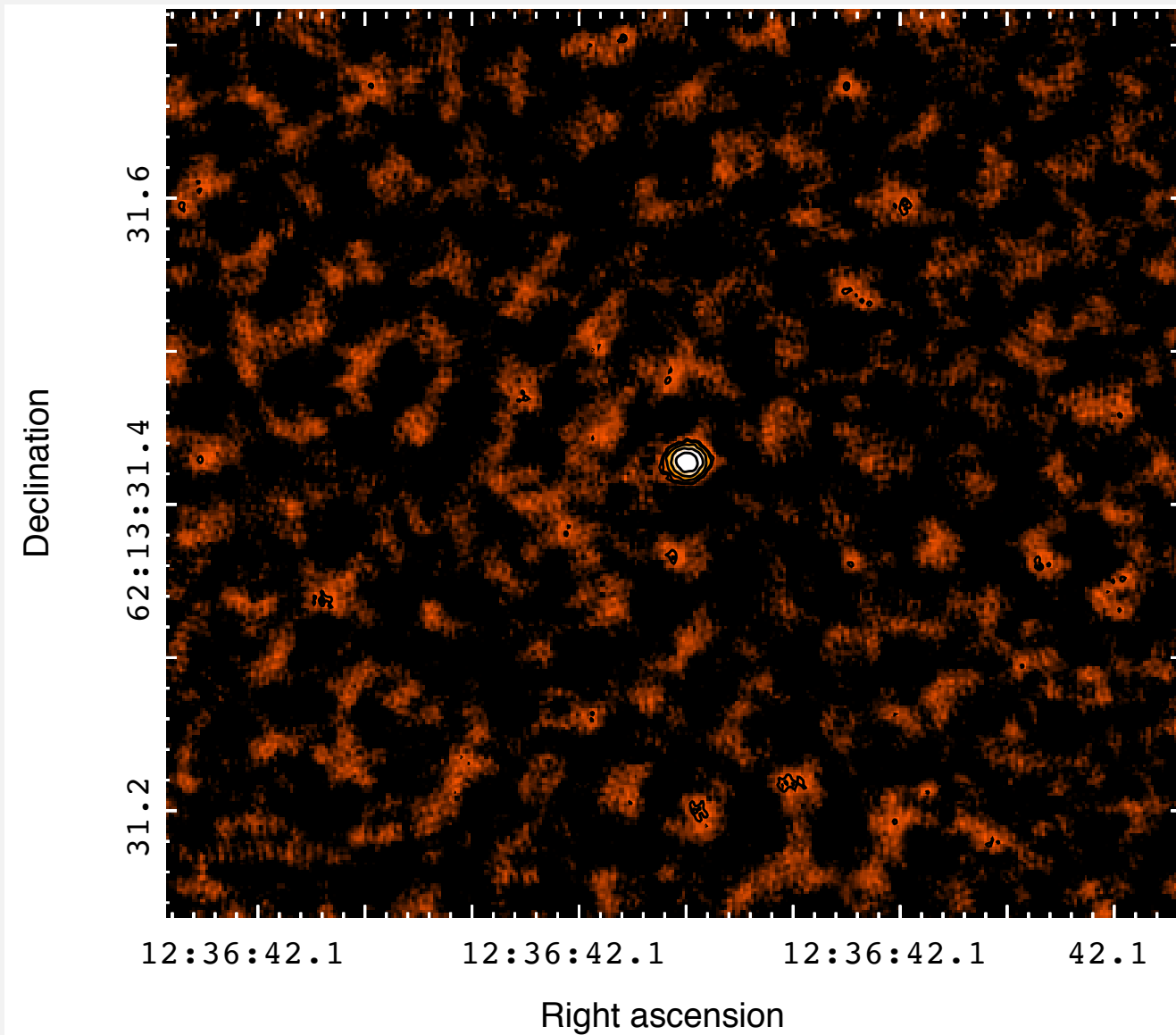
Can compromise image quality in VLBI arrays by severely restricting the  $u$ - $v$  coverage

Controlled by the `uvtaper` parameter in CASA task `tclean/clean`



# UV TAPERING

eMERLIN + EVN images of J123642+621331



### 3. WIDE-FIELD IMAGING

A 'wide-field' image is defined as:

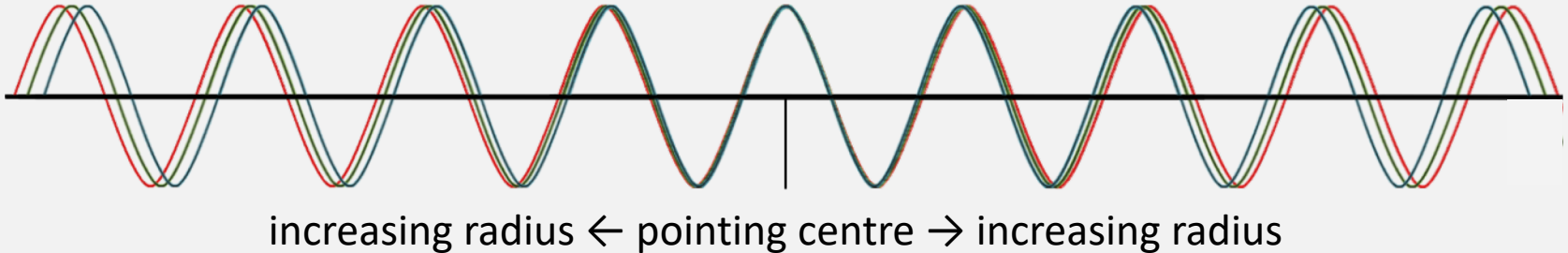
- An image with large numbers of resolution elements across them
- Or multiple images distributed across the interferometer primary beam

In order to image the entire primary beam you have to consider the following distorting effects:

1. Bandwidth smearing
2. Time smearing
3. Non-coplanar baselines (or the 'w' term) - Covered in advanced imaging
4. Primary beam response

# BANDWIDTH SMEARING

Given a finite range of wavelengths

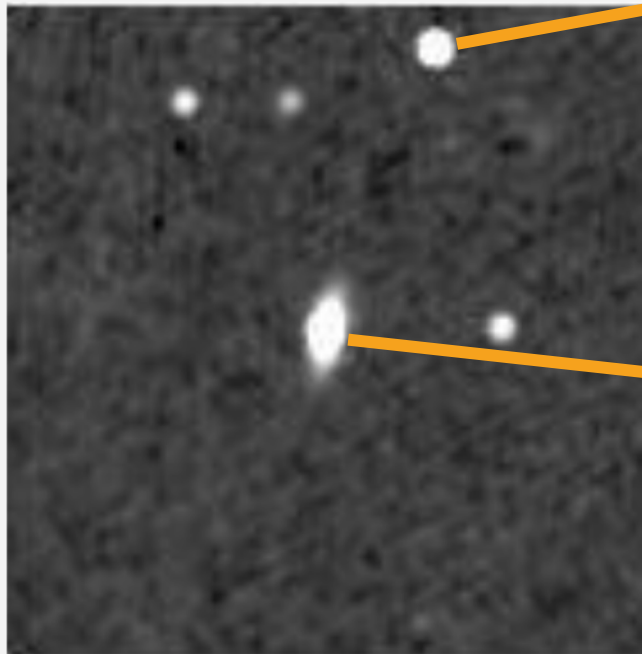


- Fringe pattern is ok in the centre but, with higher relative delay, different colours are out of phase
- BW smearing can be estimated using:  $\text{FoV} \sim \frac{\lambda}{\Delta\lambda} \frac{\lambda}{B}$
- Can be alleviated by observing and imaging with high spectral resolution with many narrow frequency channels gridded separately prior to Fourier inversion (reduces  $\Delta\lambda$ ).
- Detailed form of response depends on individual channel bandpass shapes

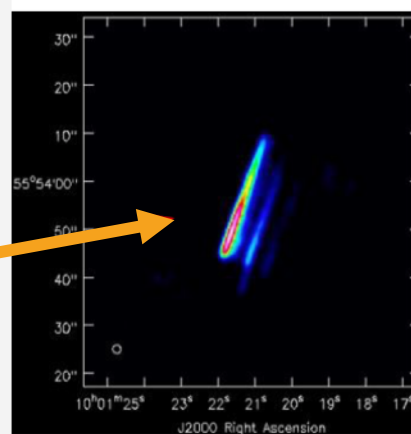
# BANDWIDTH SMEARING

Credit T. Muxlow

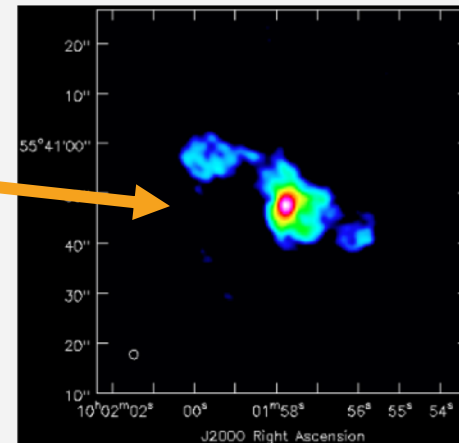
Example



NVSS image



e-MERLIN



Effect is radial smearing, corresponding to radial extent of measurements in uv plane

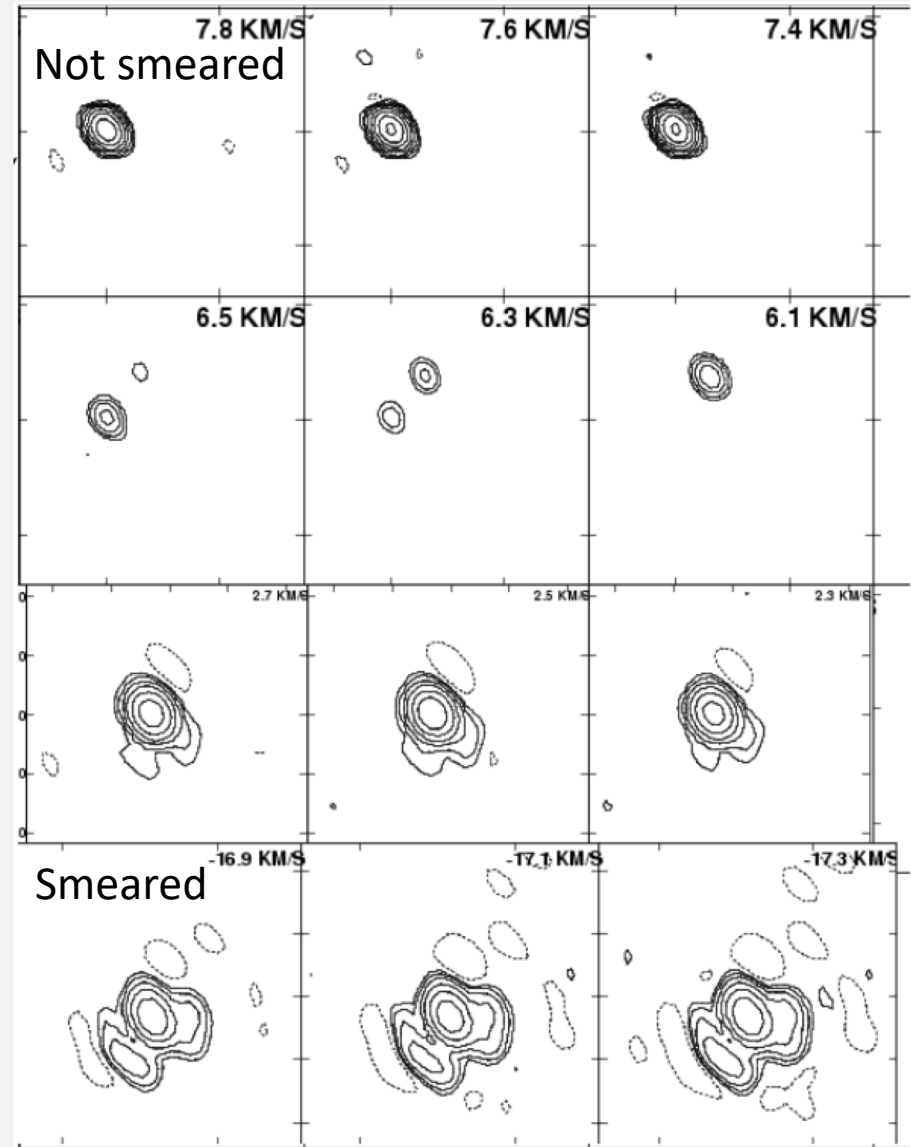
# TIME SMEARING

- Time-average smearing (de-correlation) produces tangential smearing
- Not easily parameterized. At declination  $+90^\circ$  a simple case exists where percentage time smearing is given by:

$$\omega_e \delta t_{\text{int}} \frac{\theta}{\theta_{\text{HPBW}}}$$

- At other declinations, the effects are more complicated.

Credit N. Jackson



# NON-COPLANAR BASELINES

Standard Fourier synthesis assumes planar arrays or small  $(l, m)$  - Only true for E-W interferometers e.g. WSRT

$$V(u, v, w) = \iint \frac{I(l, m)}{\sqrt{1 - l^2 - m^2}} e^{-2\pi i(ul + vm + w(\sqrt{1 - l^2 - m^2} - 1))} dl dm$$

Need to take into account the 'w' term properly in wide-fields as:

- Errors increase quadratically with offset from phase-centre
- Serious errors result if:  $\theta_{\text{offset}} [\text{rad}] \times \theta_{\text{offset}} [\text{beams}] > 1$
- Effects are severe when imaging the entire primary beam

## NON-COPLANAR BASELINES

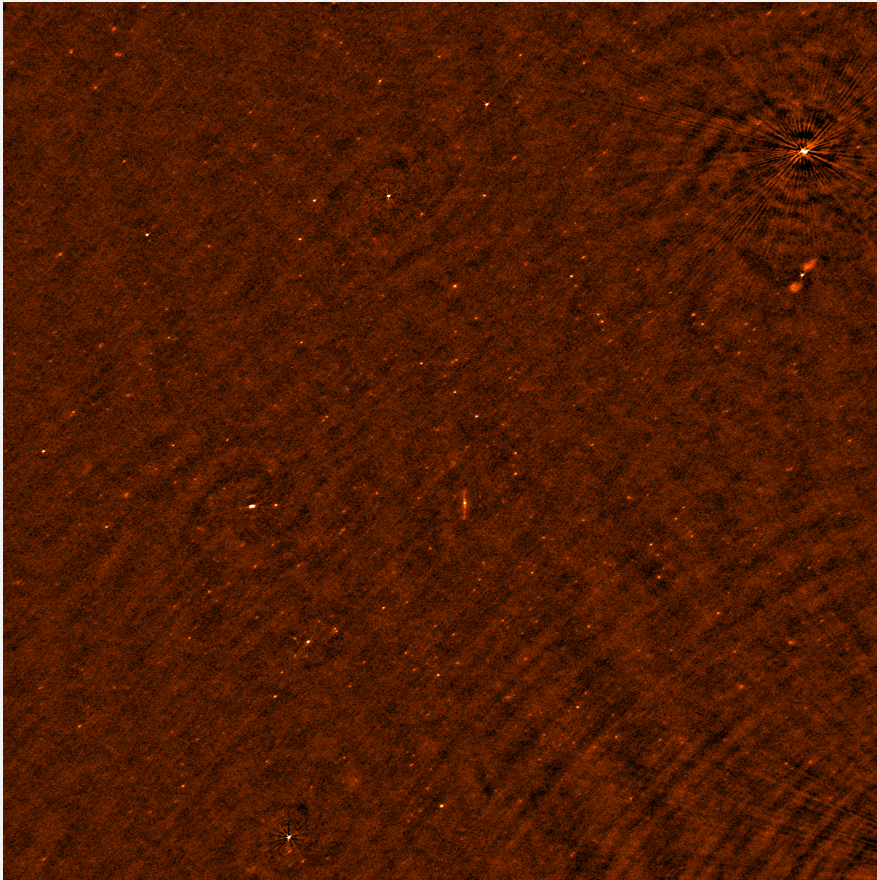
Result: We need to deal with  $V(u, v, w)$  rather than just  $V(u, v)$

Two solutions available:

- i. Faceting - split the field into multiple images to maintain  $l, m, w \sim 0$  and stitch them together.
- ii.  $w$ -projection - most used solution, project 3D sky brightness onto 2D tangent plane using  $w$  kernel.

See lecture on Advanced Imaging!

# CONFUSION



JVLA image of GOODS-N showing confusion from a 0.25Jy source to the SE

- Bright radio sources on the edge of the primary beam give rise to ripples in the centre of the field of view
- The primary beam is spectrally dependent, so image subtraction should include such corrections and be performed in full spectral-line mode
- Pointing errors introduce gain and phase changes on the edge of the primary beam. If severe, the apparent source structure may change – attempt multiple snapshot subtraction on timescales comparable with pointing error change



# CONFUSION

So how do we deal with these sources?

1. Outlier fields (the CASA default option) - deconvolve the confusing source while imaging the field of interest
2. Peeling - self-cal. on confusing source (to remove phase errors), get model & subtract source. Return to original calibration & insert model into visibilities
3. Direction-dependent calibration - see Advanced Imaging lecture

These are listed in order of complexity - note that direction dependent calibration is not available for all telescope arrays

# CONFUSION

## 1. Outlier fields

If the source is out of your desired target area, then you can set a small area around the confusing source and deconvolve with the main image.

In CASA, this is achieved by setting multiple images (see right) or set an outlier file (orange box & example below)

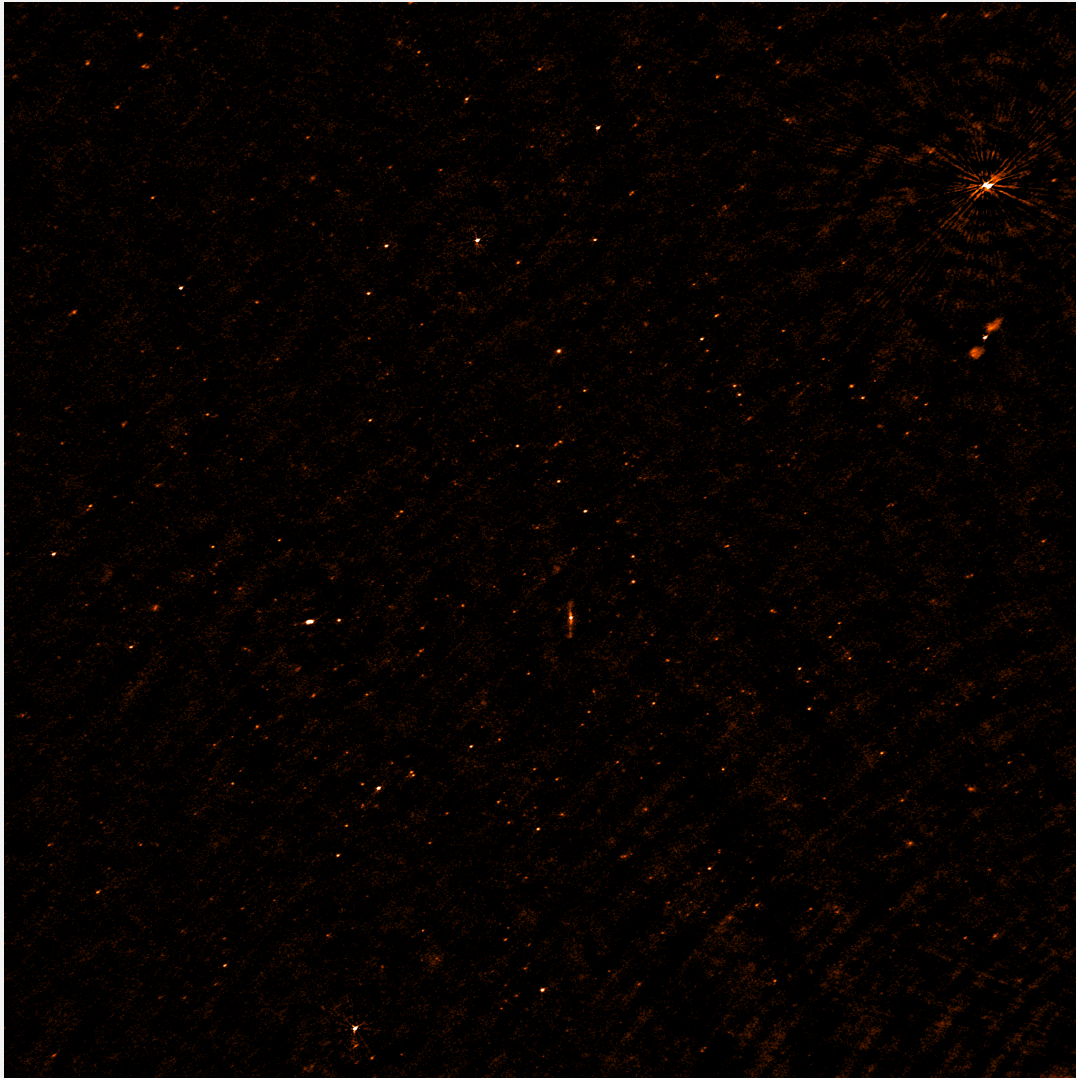
```
#content of outliers.txt
```

```
#  
#outlier field1  
imagename='outlier1'  
imsize=[512,512]  
phasecenter = 'J2000 12h34m52.2 62d02m34.53'  
mask='box[[245pix,245pix],[265pix,265pix]]'
```

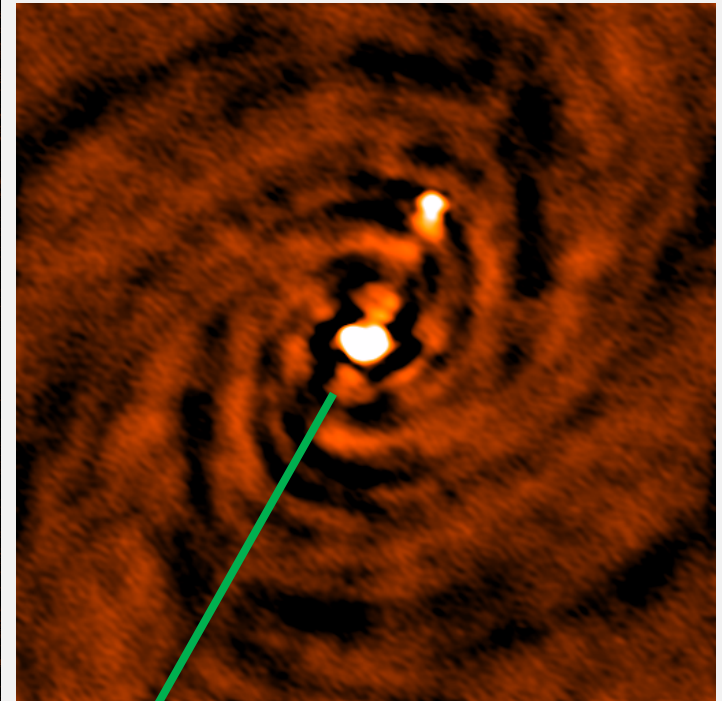
```
# clean :: Invert and deconvolve images with selected algorithm  
vis = 'JVLA_combined_GOODSN.ms' # Name of input visibility file  
imagename = ['main', 'outlier'] # Pre-name of output images  
outlierfile = '' # Text file with image names, sizes, centers for  
# outliers  
field = '' # Field Name or id  
spw = '' # Spectral windows e.g. '0~3', '' is all  
selectdata = True # Other data selection parameters  
timerange = '' # Range of time to select from data  
uvrange = '' # Select data within uvrange  
antenna = '' # Select data based on antenna/baseline  
scan = '' # Scan number range  
observation = '' # Observation ID range  
intent = '' # Scan Intent(s)  
mode = 'mfs' # Spectral gridding type (mfs, channel, velocity,  
# frequency)  
nterms = 1 # Number of Taylor coefficients to model the sky  
# frequency dependence  
reffreq = '' # Reference frequency (nterms > 1), '' uses central  
# data-frequency  
gridmode = '' # Gridding kernel for FFT-based transforms, default=''  
# None  
niter = 500 # Maximum number of iterations  
gain = 0.1 # Loop gain for cleaning  
threshold = '0.0mJy' # Flux level to stop cleaning, must include units:  
# '1.0mJy'  
psfmode = 'clark' # Method of PSF calculation to use during minor cycles  
imagermode = 'csclean' # Options: 'csclean' or 'mosaic', '', uses psfmode  
cyclefactor = 1.5 # Controls how often major cycles are done. (e.g. 5  
# for frequently)  
cyclespeedup = -1 # Cycle threshold doubles in this number of iterations  
multiscale = [] # Deconvolution scales (pixels); [] = standard clean  
interactive = False # Use interactive clean (with GUI viewer)  
mask = [] # Cleanbox(es), mask image(s), region(s), or a level  
imsize = [[8000, 8000], [50, 50]] # x and y image size in pixels. Single value:  
# same for both  
cell = ['0.33arcsec'] # x and y cell size(s). Default unit arcsec.  
phasecenter = ['J2000 12h36m49.4 62d12m58.0', 'J2000 12h34m52.2 62d02m34.53'] # Image
```

# CONFUSION

## 1. Outlier fields



0.25 Jy confusing source using outlier field assigned

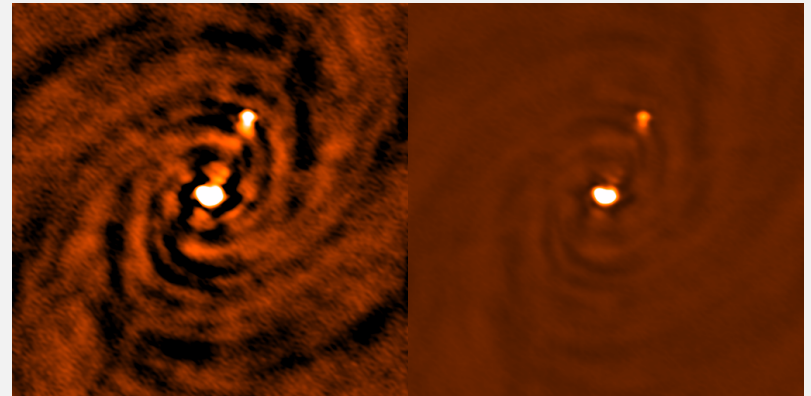
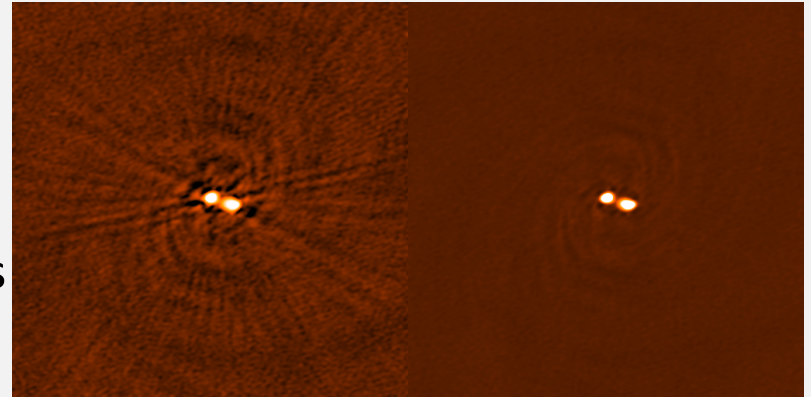


# CONFUSION

## 2. Peeling

If outlier fields do not work try peeling!

- After phase calibrating the data, perform self-calibration for the brightest confusing source – then subtract it out
- Delete phase solutions derived for previous confusing source (1)
- Move to next brightest confusing source, perform self-calibration/imaging cycles – then subtract that source from the dataset (2)
- Perform (1) and (2) until all confusing sources are subtracted. Delete all self-calibration solutions and image central regions

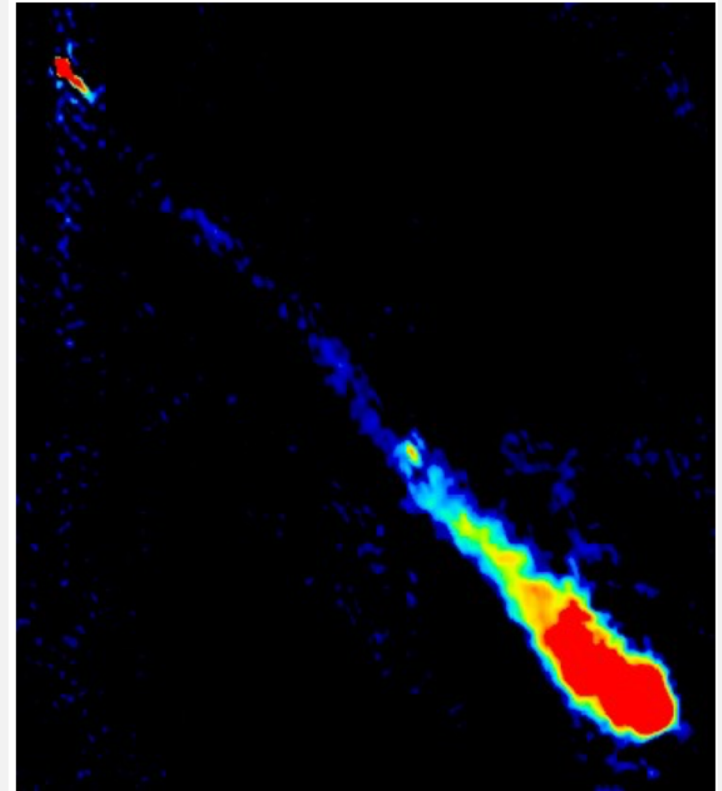


Before

After

# HIGH DYNAMIC RANGE IMAGING

- Present dynamic range limits (on axis):
  - Phase calibration – up to 1000:1 !  
improve with self-calibration
  - Non-closing data errors – continuum  
~20,000:1, line >100,000:1
  - After non-closing error correction  
~10,000,000:1
- Non-closing errors thought to be dominated by small changes in telescope passbands.
- Spectral line data configurations are the default for all new wide-band radio telescopes.
- In order to subtract out confusion we will need to be able to image with these very high dynamic ranges away from the beam centre



3C273, Davis et al. (MERLIN)  
1,000,000:1 peak – RMS

# SIGNAL TO NOISE

Noise level of a (perfect) homogeneous interferometer:

$$\text{Noise} = \frac{\sqrt{2}k_B T_{\text{sys}}}{\sqrt{n_b t \Delta\nu A \eta}}$$

where:

$T_{\text{sys}}$  - system temperature [K]

$n_b$  - number of baselines

$t$  - integration time [s]

$\Delta\nu$  - bandwidth [Hz]

$A$  - area of apertures [m]

$\eta$  - aperture efficiency

Many factors increase noise level above this value:

- Confusion
- Calibration errors
- Bad data
- Non-closing data errors
- Deconvolution artefacts

**Rarely** get this from an image. Dependent of flagging accuracy, calibration & adequate deconvolution

But techniques presented in this workshop can get you closer!